# Addressing COVID-19 Outliers in BVARs with Stochastic Volatility

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## 11th European Central Bank Conference on Forecasting Techniques

15 June 2021

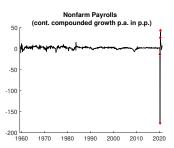
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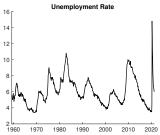
#### **RESEARCH AGENDA**

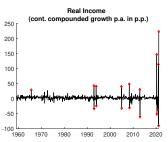
#### How to make VARs work in turbulent times?

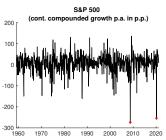
Extreme realizations since March 2020 lead to ...

- strong effects on parameter estimates
- implausible predictions in constant-variance VARs
- in terms of point and density forecasts



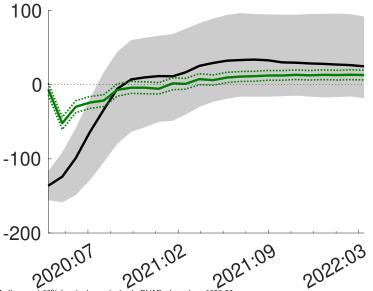






Red diamonds: outliers more than five times the IQR away from median

parameters from data through Feb (green) or Apr 2020 (black)



Medians and 68% bands, homoskedastic BVAR, data since 1959:03

#### **COVID-19 OUTLIERS AS HIGH-VARIANCE EVENTS**

- Some suggest to omit COVID-19 obs from VAR estimation (Schorfheide & Song, 2020)
- ... or to place less weight on COVID-19 data in parameter estimation (Lenza & Primiceri, 2020)

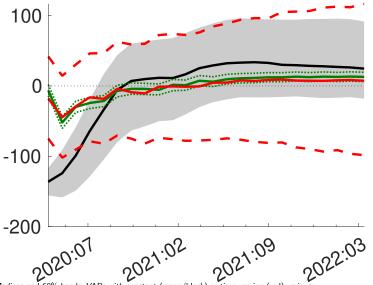
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- Some suggest to omit COVID-19 obs from VAR estimation (Schorfheide & Song, 2020)
- ... or to place less weight on COVID-19 data in parameter estimation (Lenza & Primiceri, 2020)
- Indeed, this is what VARs with SV would do: down-weight obs with larger variance of residuals
- But, conventional VAR-SV models assume changes in volatility to be highly persistent
- ... with strong effects on projected uncertainty

parameters from data through Feb (green) or Apr 2020 (black), SV (red)



Medians and 68% bands, VARs with constant (green/black) or time-varying (red) variance

#### RESEARCH AGENDA AND CONTRIBUTIONS

#### How to make VARs work in turbulent times?

Extreme realizations since March 2020 lead to ...

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- implausible predictions in constant-variance VARs
- in terms of point and density forecasts

## We develop approaches with random outliers in SV

- Outliers seen as fast, but transitory changes in SV
- Random outliers are part of the DGP and its predictions

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#### How to make VARs work in turbulent times?

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## We develop approaches with random outliers in SV

- Outliers seen as fast, but transitory changes in SV
- Random outliers are part of the DGP and its predictions

#### We also consider simple options for known outliers

- Exogenously "known" outliers
- Not modeled, not part of the DGP
- Treated with dummies, or missing-data approach

#### RELATED LITERATURE

#### Extreme data, outliers, and fat tails

- Lenza & Primiceri (2020), Schorfheide & Song (2020), Bobeica & Hartwig (2021)
- Huber, Koop, Onorante, Pfarrhofer, & Schreiner (2020),
   Guerrón-Quintana & Zhong (2020), Mitchell & Weale (2021)
- Karlsson & Mazur (2020), Jacquier, Polson, & Rossi (2004), Cúrdia, Del Negro & Greenwald (2014), Clark & Ravazzolo (2015)
- Stock & Watson (2002, 2016), Breitung & Eickmeier (2011) Artis, Banerjee, & Marcellino (2005)

#### **BVARS** with stochastic volatility

- Cogley & Sargent (2005), Primiceri (2005)
  - Carriero, Clark, & Marcellino (2019) Carriero, Chan, Clark, & Marcellino (2021)

#### **AGENDA**

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- 3 Forecasts since spring 2020
- 4 Robustness
- Conclusion
- (Appendix)

## Dynamic model for the vector $y_t$

$$y_t = \Pi_0 + \Pi(L) y_{t-1} + v_t, \qquad E_{t-1} v_t = 0$$

CONST: 
$$v_t = \Sigma^{0.5} arepsilon_t \, , \qquad \qquad arepsilon_t \sim N(0,I)$$

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 SV:  $v_t = A^{-1} \, \Lambda_t^{0.5} arepsilon_t \,, \qquad \log oldsymbol{\lambda_{j,t}} \sim RW$ 

$$A^{-1}$$
 lower unit-triangular,  $\Lambda_t$  diagonal

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 SV:  $v_t = A^{-1} \, \Lambda_t^{0.5} arepsilon_t \,, \qquad \log \lambda_{j,t} \sim RW$  SVO:  $v_t = A^{-1} \, \Lambda_t^{0.5} O_t \, arepsilon_t \,, \qquad o_{j,t} \sim iid$ 

$$o_{j,t} \sim egin{cases} 1 & ext{with prob.} & 1-p_j \ U(2,20) & ext{with prob.} & p_j \end{cases}$$

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SV: 
$$v_t = A^{-1} \, \Lambda_t^{0.5} arepsilon_t \,, \qquad \log \lambda_{j,t} \sim RW$$
SVO-t:  $v_t = A^{-1} \, \Lambda_t^{0.5} O_t \, Q_t \, arepsilon_t \,, \qquad o_{j,t}, q_{j,t} \sim iid$ 
 $q_{j,t} \sim \sqrt{IG\left(rac{
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## We consider the following variants:

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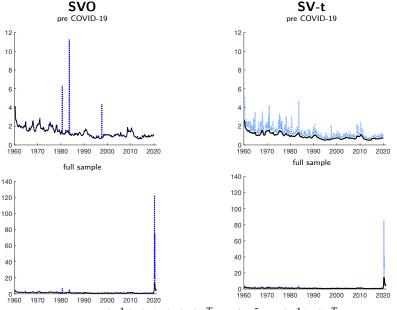
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$$o_{j,t} \sim egin{cases} 1 & ext{with prob.} & 1-p_j \ U(2,20) & ext{with prob.} & p_j \end{cases}$$
  $O_t$  can have more mass on large outliers than  $Q_t$ 

 $O_t$  can have more mass on large outliers than  $A^{-1}$  lower unit-triangular,  $\Lambda_t$ ,  $O_t$ , and  $Q_t$  diagonal

## FORECAST ERROR VOL DECOMPOSITION PAYROLL GROWTH

Total  $\Sigma_t$  incl. outliers (colored), pure SV component  $\tilde{\Sigma}_t$  (black)



Note: Medians. Total:  $\Sigma_t = A^{-1}O_tQ_t\Lambda_tQ_tO_tA^{-T}$ , pure SV:  $\tilde{\Sigma}_t = A^{-1}\Lambda_tA^{-T}$ 

## SIMPLE ALTERNATIVES TO TREAT KNOWN OUTLIERS

Two options when outlier events can be identified prior to estimation  $\dots$ 

## 1) Generic missing-data approach (SV-OutMiss)

- Pre-screen data for outliers, based on historical norms (e.g. distance from median; similar to DFM literature)
- VAR-SV with data augmentation for missing values
- Past outliers taken as given, no future outliers anticipated
- ullet Ignores outlier effects not only in estimation of  $\Pi$  but also in jump-off vector  $y_t$  for  $E_t(y_{t+h}) = \Pi^h y_t$

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#### 2) COVID-19 dummies

(SV-Dummy)

- COVID-19 generated wild swings in various months
- Separate dummies for March 2020 to March 2021
- Otherwise standard VAR-SV with wide priors on dummies (to soak up COVID data)

#### **AGENDA**

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#### SETUP OF OUR FORECAST COMPARISONS

#### **BVAR** estimation

- Non-conjugate priors (Minnesota-style shrinkage of  $\Pi$ )
- MCMC estimation with corrected triangular scheme of CCM19/CCCM21 to handle SV in larger systems
- Re-estimated for each forecast origin

#### Quasi real-time setup

- 16 variables; all data from FRED-MD 2021 April vintage
- Monthly observations since 1959:03
- Growing estimation windows
- ullet Forecasts up to two years out (h=24)

## Evaluation window 1985:01 – 2017:12 to ignore 2020 realizations

Transformation

BACKUP

**RW Prior** 

yes

Variable

Baa spread

DAIA SEI					
Monthly obs from	1959:03 to	2021:03;	FRED-MD	vintage 2021:0	4

Real Income	RPI	$\Delta \log(x_t) \cdot 1200$	
Real Consumption Exp.	DPCERA3M086SBEA	$\Delta \log(x_t) \cdot 1200$	
IP	INDPRO	$\Delta \log(x_t) \cdot 1200$	
Capacity Utilization	CUMFNS		yes
Unemployment Rate	UNRATE		yes
Nonfarm payrolls	PAYEMS	$\Delta \log(x_t) \cdot 1200$	-
Hours	CES0600000007	- , ,	
Hourly Earnings	CES0600000008	$\Delta \log(x_t) \cdot 1200$	
PPI: Finished Goods	WPSFD49207	$\Delta \log(x_t) \cdot 1200$	yes
PCE prices	PCEPI	$\Delta \log(x_t) \cdot 1200$	yes
Housing Starts	HOUST	$\log(x_t)$	yes
SP500	SP500	$\Delta \log(x_t) \cdot 1200$	
U.S. / U.K. Forex	EXUSUKx	$\Delta \log(x_t) \cdot 1200$	
5-Year yield	GS5		yes
10-Year yield	GS10		yes

**BAAFFM** 

Note: Interest-rate densities are dynamically censored at ELB

FRED-MD code

#### Values below one indicate improvement over SV SVO + SV OutMice

	SVO-t			SV-OutMiss			
Variable / Horizon	3	12	24	3	12	24	
Real Income	1.00	1.01**	0.93*				
Real Consumption	1.00	1.00	1.01				
IP	0.99	1.00	0.96***				
Capacity Utilization	0.99	1.00	0.97				
Unemployment Rate	0.99	0.99	0.99				
Nonfarm Payrolls	1.00	1.01	0.98				
Hours	1.00	0.99	1.00				
Hourly Earnings	1.00	1.01**	1.03*				
PPI (Fin. Goods)	0.99	1.00	1.00				
PCE Prices	1.00	1.01	1.03*				
Housing Starts	0.99	0.99	1.03***				
S&P 500	1.00	1.00	1.01**				
USD / GBP FX Rate	1.00	1.00	0.86				
5-Year yield	1.00	1.01	0.97				
10-Year yield	1.00	1.01	0.98				
Baa Spread	0.99	0.99	0.97				

Values below one indicate improvement over SV

	SVO-t			SV-OutMiss			
Variable / Horizon	3	12	24	3	12	24	
Real Income	1.00	1.01**	0.93*	1.00	1.01	0.94	
Real Consumption	1.00	1.00	1.01	0.99	1.00	1.00	
IP	0.99	1.00	0.96***	1.00	0.99	$0.98^{*}$	
Capacity Utilization	0.99	1.00	0.97	1.02	0.98	0.97	
Unemployment Rate	0.99	0.99	0.99	1.00	$0.99^{*}$	1.00	
Nonfarm Payrolls	1.00	1.01	0.98	1.00	0.99	0.98	
Hours	1.00	0.99	1.00	1.01	1.00	1.01	
Hourly Earnings	1.00	1.01**	1.03*	1.00	1.00	1.00	
PPI (Fin. Goods)	0.99	1.00	1.00	1.00	1.00	1.00	
PCE Prices	1.00	1.01	1.03*	0.99	1.02**	1.02	
Housing Starts	0.99	0.99	1.03***	1.00	0.99	1.00	
S&P 500	1.00	1.00	1.01**	1.00	1.00	1.01	
USD / GBP FX Rate	1.00	1.00	0.86	0.99*	1.00	0.84	
5-Year yield	1.00	1.01	0.97	0.99*	1.00	0.96	
10-Year yield	1.00	1.01	0.98	0.99	1.00	0.98	
Baa Spread	0.99	0.99	0.97	0.99	$0.99^{*}$	1.01	

Values below one indicate improvement over SV

	SVO-t			SV-OutMiss			
Variable / Horizon	3	12	24	3	12	24	
Real Income	0.96***	0.94***	0.86***	0.94***	0.94***	0.87**	
Real Consumption	0.99	$0.97^{***}$	0.91***	0.98*	0.98***	0.94**	
IP	0.99*	0.96***	0.90***	1.01	0.98***	0.96**	
Capacity Utilization	0.99	1.00	0.96	1.01	0.99	0.96**	
Unemployment Rate	1.00	1.01	1.00	0.99	0.99	0.99	
Nonfarm Payrolls	1.00	0.98*	0.93***	0.99	0.98**	0.96**	
Hours	0.99	0.98*	0.92***	1.01	0.99	$0.97^{**}$	
Hourly Earnings	0.99**	0.98***	0.93***	1.00	0.99**	0.97**	
PPI (Fin. Goods)	0.99*	0.98***	0.95***	0.99	0.99**	0.97**	
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5-Year yield	1.00	1.01*	1.01	0.99	1.00	0.99*	
10-Year yield	1.01	1.01	1.01*	1.00	1.00	0.99	
Baa Spread	0.99	0.99	$0.97^{**}$	0.98*	0.98**	$0.98^{*}$	

## TAKE AWAYS: FORECAST PERFORMANCE PRIOR 2020

Evaluating the out-of-sample forecast with origins from 1985–2017  $\dots$ 

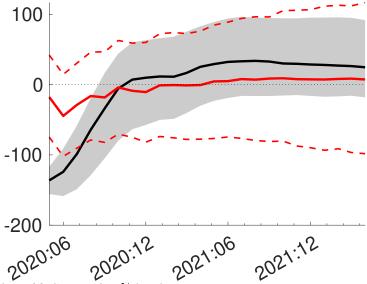
Across variables forecast horizons, we typically find:

- SVO-t did as well as, if not better, than SV
- SV outperformed the CONST benchmark (see paper)
- SV-Outmiss performed similar to SVO-t

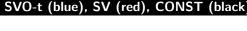
Outlier-adjusted SV helpful for outlier-prone variables while not hurting otherwise, and similarly so for missing-data treatment

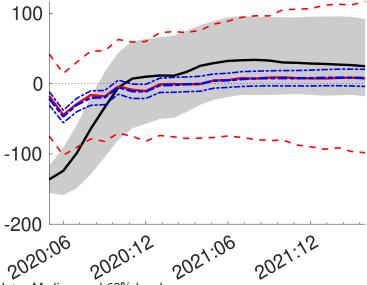
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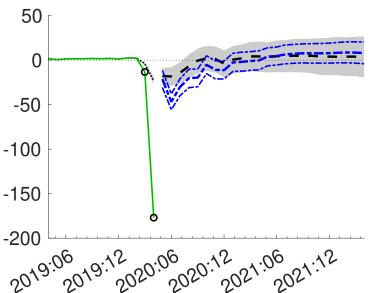


Note: Medians and 68% bands



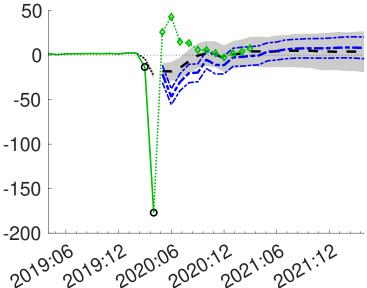


Note: Medians and 68% bands



Note: Medians and 68% bands. Circles: Pre-identified outlier data

SV-Dummies (purple), SVO-t (blue), SV-OutMiss (black), realized (green)



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## FORECAST PERFORMANCE 2020:03 – 2021:02

Typically, across all 16 variables ...

#### **Point forecasts**

- Very similar: for all of our SV variants (SV, SVO-t, SV-Dummy)
- Some differences compared to SV-Outmiss, which proved more accurate so far (RMSE, for h ≤ 6)

#### **Predictive densities**

- SV: very wide
- SV-Dummy: extremely tight
- SVO-t and SV-OutMiss: in between
- Some advantage of SVO-t over SV, (CRPS  $h \le 6$ ) with SV-Outmiss at least as strong

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#### Caveat: Only few realizations observed so far

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#### ROBUSTNESS

In paper and appendices we also consider ...

## Variants of outlier-adjusted SV: SVO and SV-t

- Close performance, on average, in the pre-2020 sample for point and density forecasts
- SVO a little weaker than SVO-t at longer horizons, and SV-t quite close to SVO-t

# Common vs variable-specific outliers

ullet Common outlier posits one scalar factor,  $o_t$ , that simultaneously scales all variables up or down

$$v_t = o_t \cdot A^{-1} \Lambda_t^{0.5} arepsilon_t \qquad \qquad arepsilon_t \sim N(0,I)$$

- Maybe ok for tightly selected variables during COVID-19
- Less plausible for broader set of variables

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#### CONCLUSIONS

## Benefits of outlier-adjusted SV in BVARs

- Detects outliers as random, not known, events
- Delineates transitory spikes from persistent changes in SV
- Pre-COVID-19: a little better, no worse than regular SV
- Since COVID-19: more plausible forecast densities

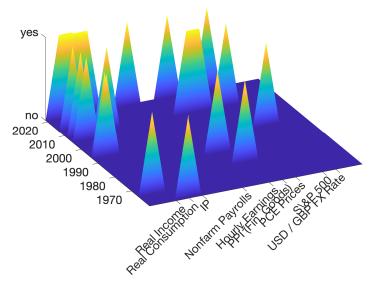
## Alternative: missing-data approach

- Require outliers to be known/identified ex-ante
- Outliers not modeled, densities assume standard VAR-SV
- Robust performance

### Makes BVARs work through turbulent times

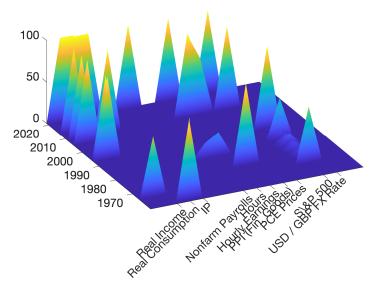
- Outliers in post-war data
- Specification of SVO vs SV-t models
- Individual vs common outliers
- Payroll forecasts in 2020/2021
- Forecast errors since COVID-19

Occurrence of observations more than 5 times the IQR away from median



Measured over full sample of monthly data 1959:03-2021:03. Later we use growing samples in quasi-real time.

Odds of observations counted as outlier in growing samples starting 1985



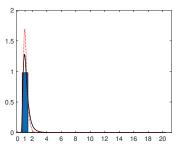
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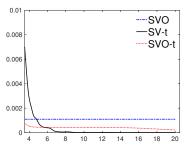
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### $o_t$ can place more mass on large outliers than $q_t$







- SVO prior sees 1 outlier every 4 years
- For SVO-t: prior mean lowered to 1 outlier every 10 years
- Here: SV-t and SVO-t calibrated to same variance as SVO (will be estimated in our empirical application)

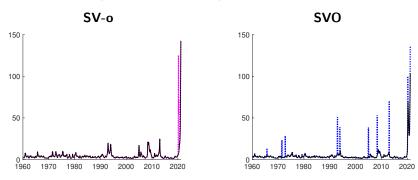
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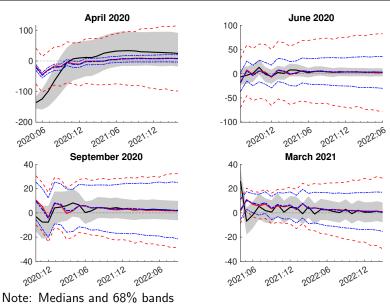
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- Less plausible for broader set of variables
- For example, FE vol decomposition for real income:



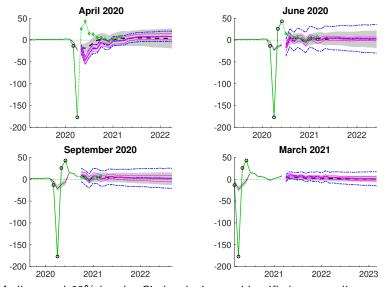
- Outliers in post-war data
- Specification of SVO vs SV-t models
- Individual vs common outliers
- Payroll forecasts in 2020/2021
- Forecast errors since COVID-19

## PAYROLL GROWTH FORECASTS SVO-t (blue), SV (red), CONST (black)



## PAYROLL GROWTH FORECASTS W/KNOWN OUTLIERS

SV-Dummies (magenta), SVO-t (blue), SV-OutMiss (black), realized

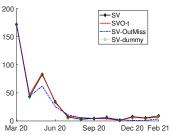


Medians and 68% bands. Circles depict pre-identified past outliers

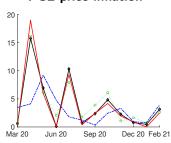
- Outliers in post-war data
- Specification of SVO vs SV-t models
- Individual vs common outliers
- Payroll forecasts in 2020/2021
- Forecast errors since COVID-19

Absolute errors of one-step ahead forecasts made March 2020 to Feb 2021

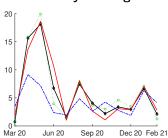
# Payroll growth



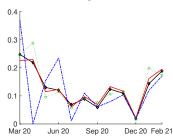
## PCE price inflation



#### **Hourly Earnings**



#### Housing starts



#### CONCLUSIONS

## Benefits of outlier-adjusted SV in BVARs

- Detects outliers as random, not known, events
- Delineates transitory spikes from persistent changes in SV
- Pre-COVID-19: a little better, no worse than regular SV
- Since COVID-19: more plausible forecast densities

## Alternative: missing-data approach

- Require outliers to be known/identified ex-ante
- Outliers not modeled, densities assume standard VAR-SV
- Robust performance

## Makes BVARs work through turbulent times