Combining Bayesian VARs with survey density forecasts: does it pay off?

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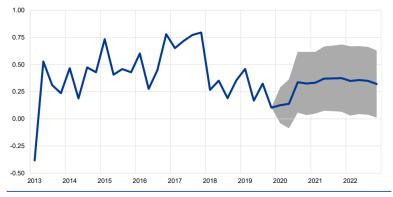
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Euro area real GDP



(quarter-on-quarter percentage changes, seasonally and working day-adjusted quarterly data)

Notes: The ranges shown around the projections are based on the differences between actual outcomes and previous projections carried out over a number of years. The width of the ranges is twice the average absolute value of these differences. The method used for calculating the ranges, involving a correction for exceptional events, is documented in "New procedure for constructing Eurosystem and ECB staff projection ranges", ECB, December 2009, available on the ECB's website.

Source: Eurosystem staff macroeconomic projections for the euro area, March 2020.

Summary

- Bayesian VARs a standard tool for computing density forecasts. Moreover, model uncertainty and absence of forward-looking information are issues.
- We estimate in real-time a wide range of model specifications on European data, then optimally combine the forecast densities.
- We incorporate forward-looking survey information:
 - Tilt first each individual model, then perform optimal pooling ("ex-ante");
 - Tilt directly the combined density obtained from optimal pooling ("ex-post").
 - Include the SPF as additional prediction.
- 1. **Optimally combining several models** improves overall point and density performance, as well as forecast calibration.
- 2. **Including survey forecasts** on the target's **mean** helps, while on the variance hinders, overall performance.
- Ex-ante performs well → scope for improving ex-ante models and then combine.

BVARs, combinations and SPF

BVAR model types: Minnesota priors with SV; democratic priors with SV; (Survey) Local Mean with SV; TVP-SV; UCSV. Different data set compositions: 3 or 19 variables, aggregated euro area or by country. 13 models and it can be extended to other specifications.

EU SPF.

- Optimal linear predictive pool.
- Combining survey and model information: "ex-ante" and "ex-post" tilting.
- Target variables: y-o-y growth rate of euro area HICP inflation and GDP, evaluated at 1- and 2-year ahead horizon.
- Real-time recursive estimation, with forecasts evaluated from 2000:Q1 to 2019:Q4.

Combination performance - GDP

	Optimal Pool: <i>abs.</i> <i>scores</i>	SPF	Opt. Pool w/SPF	μ tilted ex- ante	μ tilted ex- post	$\mu \& \sigma$ tilted ex- ante	μ&σ tilted ex- post
4-q CRPS LPS PITS	0.808 -1.922 0.042	0.994 -0.627 0.000	0.997 0.030 0.016	0.935 0.302 0.624	0.932 0.026 0.279	0.966 -0.406 0.000	0.971 -0.485 0.000
8-q CRPS LPS PITS	0.994 -1.973 0.020	1.091 -1.112 0.000	1.001 -0.094 0.011	1.080 -0.042 0.099	1.033 -0.095 0.004	1.102 -1.243 0.000	1.099 -1.303 0.000

Table: Relative accuracy scores with respect to optimal pooling (i.e. first column); p-values of Berkowitz uniformity test (in absolute terms).

Combination performance - HICP

Optima Pool: <i>abs.</i> <i>scores</i>	I SPF	Opt. Pool w/SPF	μ tilted ex- ante	μ tilted ex- post	$\mu \& \sigma$ tilted ex- ante	$\mu \& \sigma$ tilted ex- post
4-q CRPS 0.503 LPS -1.306 PITs 0.839	0.932 -0.024 0.002	0.991 0.003 0.704	0.917 0.117 0.218	0.937 0.056 0.156	0.943 -0.007 0.000	0.944 -0.082 0.000
8-q CRPS 0.567 LPS -1.429 PITs 0.552	0.949 -0.040 0.000	1.020 -0.001 0.961	0.922 0.082 0.368	0.941 0.032 0.232	0.964 -0.263 0.000	0.963 -0.284 0.000

Table: Relative accuracy scores with respect to optimal pooling (i.e. first column); p-values of Berkowitz uniformity test (in absolute terms).

Combination performance - Bivariate

	Optimal Pool: <i>abs.</i> <i>scores</i>	SPF	Optimal Pool with SPF	μ- tilted ex- ante	μ- tilted ex- post	μ and $\sigma\text{-}$ tilted ex- ante	μ and σ - tilted ex- post
4-q							
ES	1.015	0.995	0.987	0.961	0.954	0.983	0.984
LPS	-3.355	-0.416	0.144	0.433	0.220	-0.106	-0.352
PITs y∣h	0.538	0.000	0.907	0.690	0.650	0.000	0.000
PITs h∣y	0.026	0.013	0.078	0.219	0.168	0.002	0.001
8-q							
ES	1.254	1.054	0.989	1.024	1.016	1.069	1.068
LPS	-3.766	-0.501	0.061	0.233	-0.017	-0.782	-0.874
PITs y∣h	0.214	0.000	0.623	0.721	0.185	0.000	0.000
PITs h y	0.075	0.002	0.156	0.707	0.225	0.000	0.000